

Ana 1 - Blatt 13

Aufg. 1 - Unbestimmte Integrale

$$(3) \int x \cdot \arcsin(x) dx = \left[ \frac{1}{2} x^2 \cdot \arcsin(x) \right] - \int \frac{1}{2} x^2 \cdot \frac{1}{(1-x^2)^{\frac{1}{2}}} dx$$

$\uparrow$   $\uparrow$   $\uparrow$   $u \cdot v$   $u \cdot v'$   
 $u'$   $v$

$$\left(\frac{1}{2}x^2\right)' = \frac{2}{2}x = x$$

$$(\arcsin(x))' = \frac{1}{(1-x^2)^{\frac{1}{2}}} = \frac{1}{\sqrt{1-x^2}}$$

$$= \left[ \frac{1}{2} x^2 \cdot \arcsin(x) \right] - \int \frac{1}{2} x^2 \cdot \frac{1}{\sqrt{1-x^2}} dx = \left[ \frac{1}{2} x^2 \arcsin(x) \right] - \int \frac{1}{2x} \cdot \frac{dz}{2x}$$

$$z' = 2x = \frac{dz}{dx} \cdot 1 \cdot dx$$

$$2x dx = dz \quad | : 2x$$

$$dx = \frac{dz}{2x}$$

$$= \left[ \frac{1}{2} x^2 \arcsin(x) \right] - \int \frac{x^2}{2} \cdot \frac{1}{2x \cdot z^{\frac{1}{2}}} dz = \left[ \frac{1}{2} x^2 \arcsin(x) \right] - \int \frac{1}{2z^{\frac{1}{2}}} dz$$

?????  
(Substitution)  
 $z = 1 - x^2$

Wie geht's weiter???